

## Quiz 8: Bounds on Information Processing

**Question 1.** Which of the following states has the largest value of  $I(A : B)$ ?

- (a)  $\rho_{AB} = |0_A\rangle\langle 0_A| \otimes |1_B\rangle\langle 1_B|$ .
- (b) The maximally mixed state.
- (c) The maximally correlated state.
- (d) The maximally entangled state.

**Question 2.** Which of the following states has the largest value of  $H(A|B)$ ?

- (a)  $\rho_{AB} = |0_A\rangle\langle 0_A| \otimes |1_B\rangle\langle 1_B|$ .
- (b) The maximally mixed state.
- (c) The maximally correlated state.
- (d) The maximally entangled state.

**Question 3.** For which of the following classes of states does monotonicity,  $H(AB) \geq H(A)$ , hold?

- (a) Classical states.
- (b) Product states.
- (c) Pure states.

**Question 4.** Suppose Alice and Bob share a state between systems  $A$  and  $B$ . Which of the following are true?

- (a) Alice cannot increase  $I(A : B)$  by performing operations on her system.
- (b) Alice cannot increase  $I(A : B)$  by sending Bob classical information.

**Question 5.** Suppose Alice and Bob share a maximally entangled state of dimension  $d$ . They perform some operations individually on their systems without communicating. Which of the following states can they produce?

- (a) A maximally entangled state of dimension  $d + 1$ .
- (b) A maximally mixed state of dimension  $d + 1$ .
- (c) A maximally correlated state of dimension  $d$ .